

Domain Adaptation for Visual Applications

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Outline

1. Introduction

Benchmark Datasets

2. Main domain adaptation methods

Instance reweighing methods

Parameter based methods

Feature transformation-based methods

3. Combined methods

Joint feature transform and parameter adaptation

Joint feature/instance selection and feature transform

Joint instance selection, feature and parameter adaptation

4. Heterogeneous features

5. Multiple sources

6. Deep Learning

7. Conclusion and Perspectives

Domain Adaptation (DA)

Leveraging labeled data in one or more related domains, referred to as **source domains**, to learn a classifier for unseen data in a **target domain**.

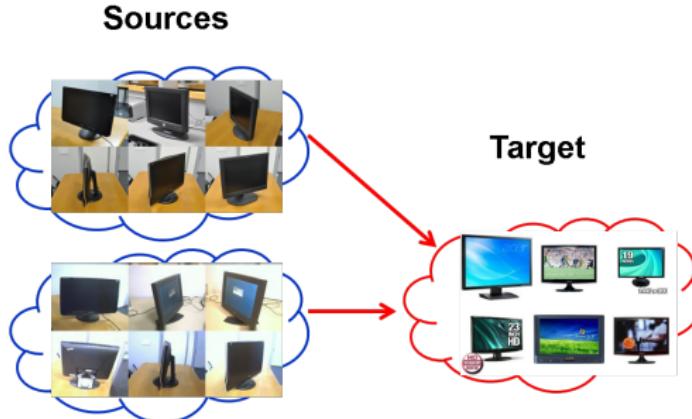


Image: Courtesy to S.J. Pan

- ▶ Unsupervised (US) DA when no label is available for the target
- ▶ Semi-supervised (SS) DA when we have a few labels in the target

Transfer Learning

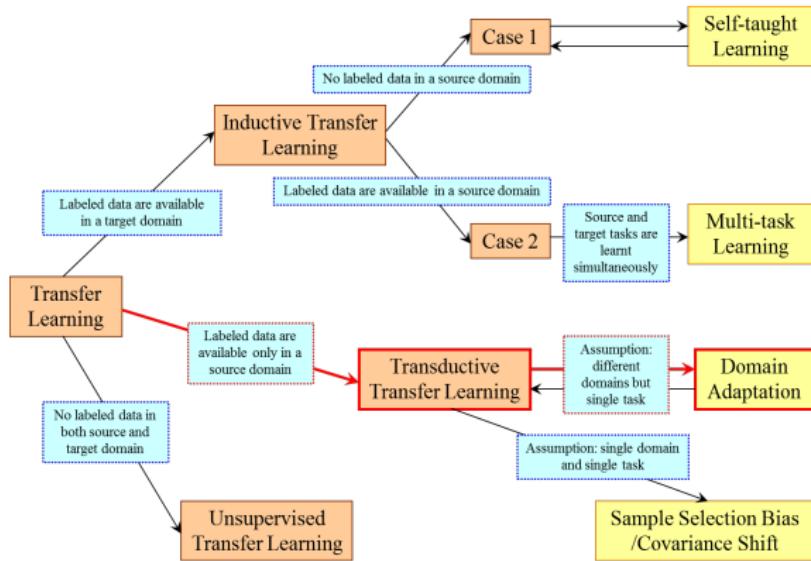


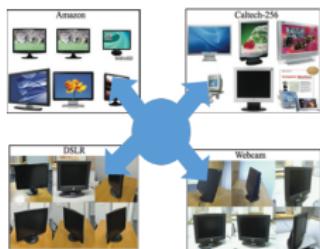
Image: Courtesy to S.J. Pan

Particular case of the transductive transfer learning where

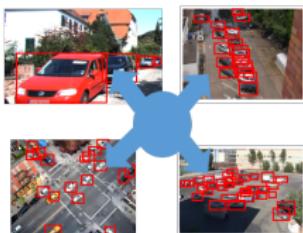
- ▶ domains are different but the task is the same (e.g. same classes)

Example scenarios

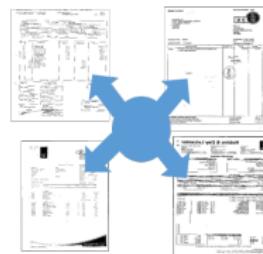
Object recognition



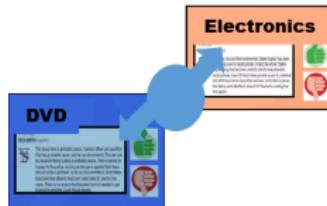
Object detection



Document image categorization



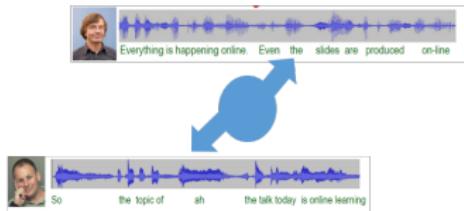
Sentiment analyses



Action recognition



Speech recognition



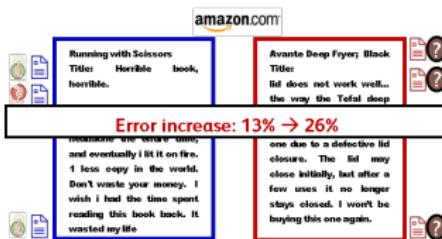
Why not just use source model?

Statistical Machine Translation

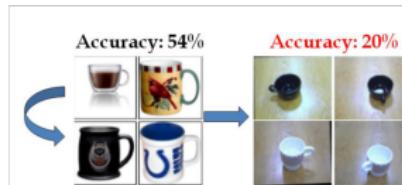
- Source Domain
 - European Parliament Text
- Target Domain:
 - Research Articles in Social Sciences.
- No Adaptation
 - 28% Mean Average Precision (MAP)
- With Adaptation 34%

- German query:
Selbstmord von Jugendlichen
- Baseline translation:
suicide of young (MAP = 0.3210)
- Adaptation:
suicide of adolescents (MAP = 0.5277)

Sentiment analyses



Object recognition



Applying the models learned on the source directly often performs poorly!

Domain shift/distribution mismatch

Underlying causes:

- ▶ Image categorization
 - different point of views, acquisition time and conditions,
- ▶ Audio recognition
 - different persons, environment, recording quality
- ▶ Document image categorization
 - differences in appearance, layout
- ▶ Activity recognition
 - different persons, environment, context
- ▶ Semantic analyses
 - different topics, vocabularies, ...

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Amazon review dataset¹ (AMT)



Products reviews in different domains

- ▶ kitchen (K), dvd (D), books (B) and electronics (E)
- ▶ 2 classes, about 5,000 document for each class
- ▶ TFIDF from processed text

¹ Blitzer *et al.*, Domain adaptation with coupled subspaces, AIS11

Office31² (OFF31) & Office+Caltech³ (OC10)



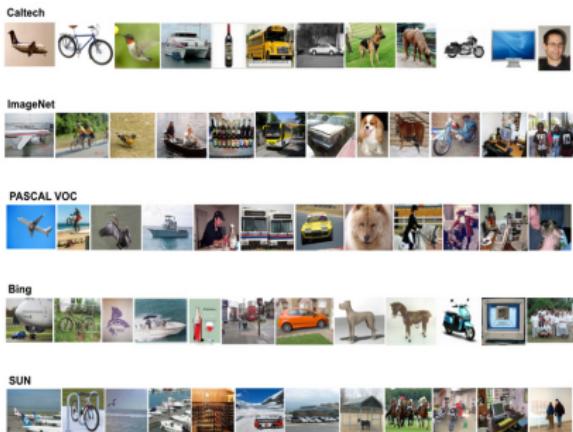
Object recognition:

- ▶ Amazon (A), Caltech (C) , Dslr (D) , Webcam (W)
- ▶ 3 domains and 31 classes in OFF31 and 4 domains and 10 classes in OC10
- ▶ SURF BOV and Decaf6 (CNN activation) features
 - using all source examples (ase)
 - using several subset of the source data and average(sse)

²Saenko *et al.*, Adapting visual category models to new domains, ECCV10

³Gong *et al.*, Reshaping visual datasets for domain adaptation, NIPS13

The ImageCLEF'14 DA Challenge⁴ (ICDA)



Object recognition:

- ▶ Caltech (C), ImageNet (I), Pascal (P), Bing (B), SUN (S)
- ▶ 12 classes, about 60 document for each class
- ▶ SIFT BOV features from images

⁴ <http://www.imageclef.org/2014/adaptation>

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Different solutions

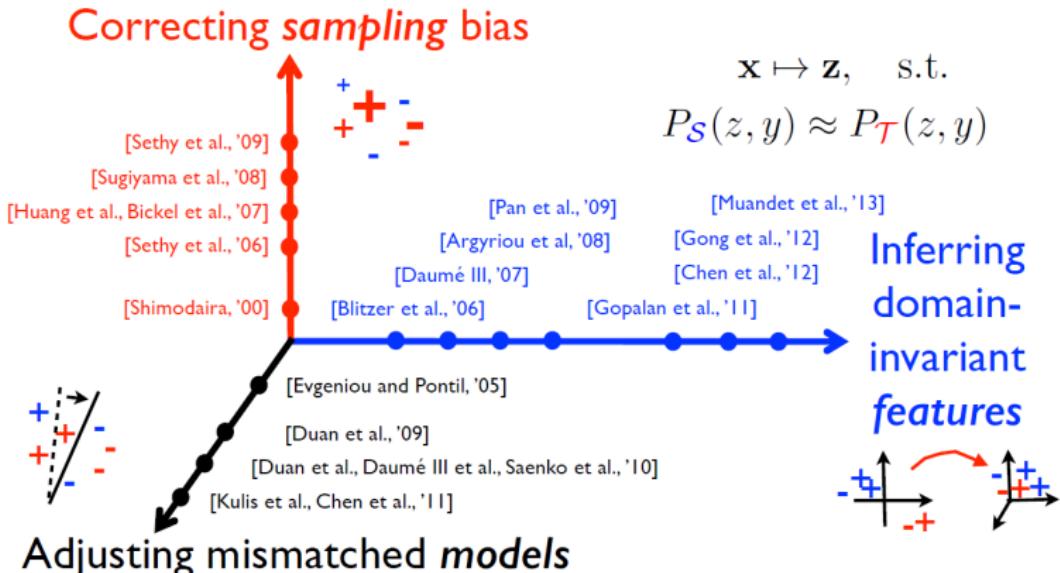


Image: Courtesy to Boqing Gong.

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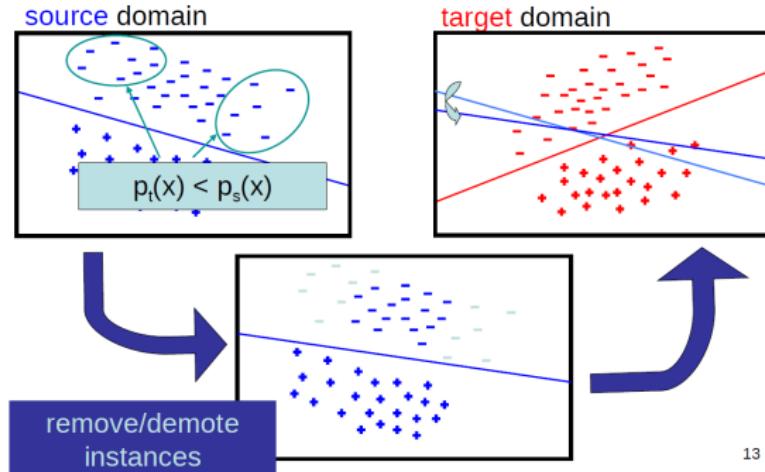
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Correcting sampling bias



13

Image: Courtesy to Ming-Wei Chang.

Learn a classifier such that

- ▶ more weights are put on the examples that are similar to target instances
- ▶ less weights (or removing) on those that are less similar

How to estimate the weights

- ▶ Using the classifier that distinguishes between source and target examples (Bickel *et al.* ICML'07)

$$\alpha(\mathbf{x}_i^s) = \frac{1}{p(y_i^s = s | \mathbf{x}_i^s, \theta)}$$

- ▶ considering the ratio between the densities estimated for source and target domains (Sugiyama *et al.* NIPS'07, Kanamori *et al.* JMLR'09)

$$\alpha(\mathbf{x}) = \frac{P_T(\mathbf{x})}{P_S(\mathbf{x})} \approx \sum_I \alpha_I \phi_I(\mathbf{x})$$

Maximum Mean Discrepancy

- ▶ Minimizing the Maximum Mean Discrepancy (Huang *et al.* NIPS'06)

$$MMD(S, T) = \left\| \frac{1}{N_s} \sum_{i=1}^{N_s} \phi(\mathbf{x}_i^s) - \frac{1}{N_t} \sum_{j=1}^{N_t} \phi(\mathbf{x}_j^t) \right\|_{\mathcal{H}}$$

where \mathcal{H} is the RKHS (reproducing kernel Hilbert space) associated with the kernel k , and $\phi(\mathbf{x}) = \langle k(\mathbf{x}), \cdot \rangle$.

- ▶ Empirically:

$$MMD(S, T) = \left[\frac{1}{N_s^2} \sum_{i,j=1}^{N_s} k(\mathbf{x}_i^s, \mathbf{x}_j^s) - \frac{2}{N_s N_t} \sum_{i,j=1}^{N_s, N_t} k(\mathbf{x}_i^s, \mathbf{x}_j^t) + \frac{1}{N_t^2} \sum_{j,j=1}^{N_t} k(\mathbf{x}_j^t, \mathbf{x}_j^t) \right]$$

with k being e.g. the Gaussian Kernel.

Transfer Adaptive Boosting⁵

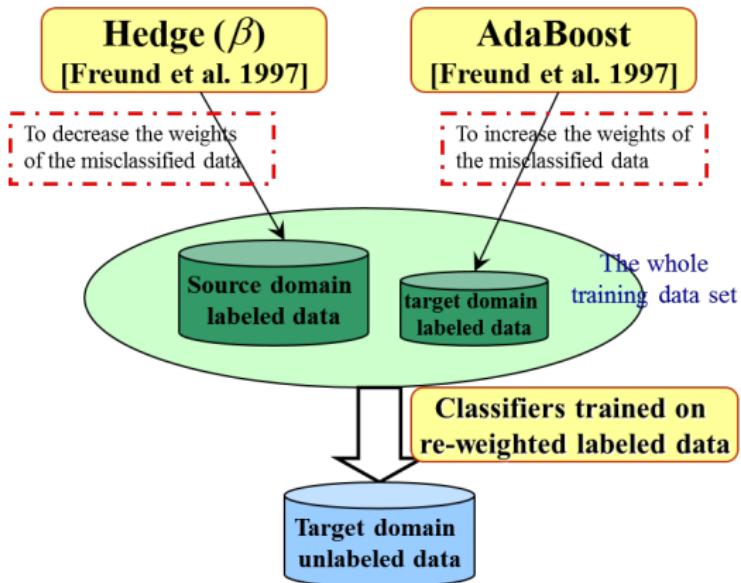


Image: Courtesy to S.J. Pan.

⁵ Dai et al., Boosting for transfer learning, ICML'07.

TrAdaBoost result

- ▶ 20 Newsgroups - text categorization across newsgroups.
- ▶ Abalone - seven physical measurements of abalone sea snails.
- ▶ Wine - red wine physical and chemical characteristics versus white wine.

Dataset	AdaBoost	TrAdaBoost	Fixed-Cost (1.1,1.2,1.3)	Dynamic
Sci vs Talk	0.552	0.577	0.581	0.618
Rec vs Sci	0.546	0.572	0.588	0.631
Rec vs Talk	0.585	0.660	0.670	0.709
Wine Quality	0.586	0.604	0.605	0.638
Abalone Age	0.649	0.689	0.682	0.740

- **TrAdaBoost** - Transfer Adaptive Boosting, Dai *et al.*, ICML'07.
- **Dynamic** - Dynamic updates for TrAdaBoost, Al-Stouhi and Reddy, PKDD'11.

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Adaptive SVM⁶ (A-SVM)

Adaptive SVM [Yang et al. MM 2007]

$$f^s(\mathbf{x}) + \Delta f(\mathbf{x}) = f^t(\mathbf{x})$$

Source Classifier Perturbation function Target classifier

The diagram illustrates the composition of classifiers. On the left, a box labeled "Source Classifier" contains a minus sign above a plus sign. In the middle, a box labeled "Perturbation function" contains a plus sign below a minus sign. To the right, a box labeled "Target classifier" contains a plus sign above a minus sign. A plus sign is placed between the first two boxes, and an equals sign is placed between the second and third boxes.

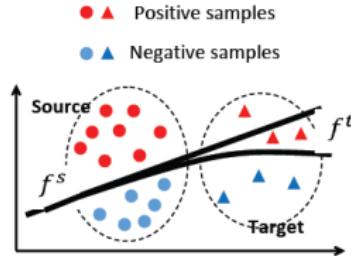


Image: Courtesy to Dong Xu.

The target classifier:

$$f^t(\mathbf{x}) = \sum_{k=1}^M \beta_k f_k^a(\mathbf{x}) + \sum_{i=1}^N \hat{\alpha}_i y_i K(\mathbf{x}, \mathbf{x}_i)$$

leverages multiple auxiliary classifiers f_k^a .

⁶ Yang et al., Cross-domain video concept detection using adaptive SVMs, MM'07

Domain Adaptation SVM⁷ (DASVM)

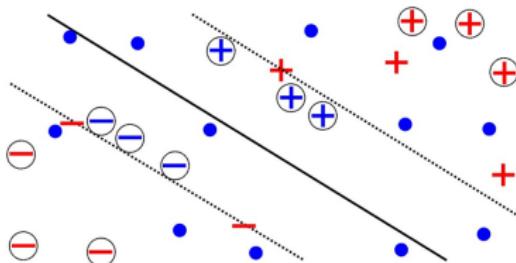


Image: Courtesy to Amaury Habrard.

Adapt iteratively (until stopping criteria reached) the classifier built with the source:

- ▶ add to negatives the first k predicted target $h(\mathbf{x}_t) > 0$ with highest margin
- ▶ add to positives the first k predicted target $h(\mathbf{x}_t) < 0$ with highest margin
- ▶ remove the first k positive and k negative source instances with highest margin

⁷ Bruzzone and Marconcini, Domain Adaptation Problems: A DASVM Classification Technique and a Circular Validation Strategy PAMI'10.

Adaptive MKL⁸

- Proposed formulation of A-MKL

Structural risk functional

$$\min_{\mathbf{d}} G(\mathbf{d}) = \frac{1}{2} \cdot \text{MMD}^2(\mathbf{d}) + \theta \cdot J(\mathbf{d})$$

where $J(\mathbf{d}) = \min_{\mathbf{w}_m, \beta, b, \xi_i} \frac{1}{2} \left(\sum_{m=1}^M d_m \|\mathbf{w}_m\|^2 + \lambda \|\beta\|^2 \right) + C \sum_{i=1}^n \xi_i$

s. t. $y_i \cdot f^t(\mathbf{x}) \geq 1 - \xi_i, \xi_i \geq 0$ Regularization
Hinge loss

- Dual form of $J(\mathbf{d})$

$$\min_{\alpha} -\alpha^\top \mathbf{1} + \frac{1}{2} (\alpha \circ \mathbf{y})^\top \left(\sum_{m=1}^M d_m \tilde{\mathbf{K}}_m \right) (\alpha \circ \mathbf{y}) \quad \text{s. t. } \begin{aligned} \alpha^\top \mathbf{y} &= 0, \\ \mathbf{0} &\leq \alpha \leq C \mathbf{1} \end{aligned}$$

where $\tilde{\mathbf{K}}_m(\mathbf{x}_i, \mathbf{x}_j) = \mathbf{K}(\mathbf{x}_i, \mathbf{x}_j) + \frac{1}{\lambda} \sum_{p=1}^P f_p(\mathbf{x}_i) f_p(\mathbf{x}_j)$

Solution:
Iteratively
optimize \mathbf{d} and
solve the SVM
problem.

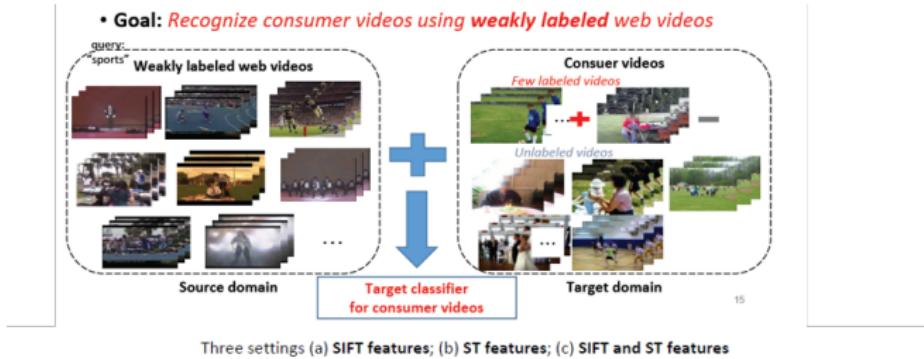


Image: Courtesy to D. Xu.

⁸

Duan et al. Visual Event Recognition in Videos by Learning from Web Data, CVPR'10.

Video event recognition



Means and standard deviations of mean average precision (%) over six classes

	SVM_T	SVM_AT	FR	A-SVM	MKL	DTSVM	A-MKL
MAP-(a)	42.32 ± 5.50	53.93 ± 5.58	49.98 ± 5.63	38.42 ± 7.93	47.19 ± 2.59	52.36 ± 1.88	57.14 ± 2.34
MAP-(b)	32.56 ± 2.08	24.73 ± 2.22	28.44 ± 2.61	24.95 ± 1.25	35.34 ± 1.55	31.07 ± 2.60	37.24 ± 1.58
MAP-(c)	42.00 ± 4.94	36.23 ± 3.37	44.11 ± 3.57	32.40 ± 4.99	46.92 ± 2.53	53.78 ± 2.99	58.20 ± 1.87

Image: Courtesy to D. Xu.

- **A-SVM** - Adaptive SVM, Yang *et al.* MM'07.
- **DTSVM** - Domain Transfer SVM, Duan, CVPR'09.
- **A-MKL** - Adaptive Multiple Kernel Learning, Duan *et al.* CVPR'10.

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Feature space transformation

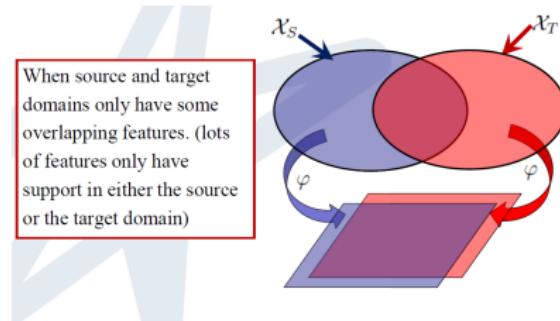


Image: Courtesy to Dong Xu.

Unsupervised feature transform

- ▶ Align pivot features (Biltzer *et al.* EMNLP'06, Pan *et al.* WWW'10)
- ▶ Manifold based methods (Pan *et al.* IJCAI'09, Gong *et al.* CVPR'12)
- ▶ Unsupervised subspace alignment (Fernando *et al.* ICCV'12)
- ▶ Stacked Marginalized Denoising Autoencoders (Chen *et al.* ICML'12)

Semi-supervised feature transform

- ▶ Metric learning based approaches (Zha *et al.* IJCAI'09, Saenko *et al.* ECCV'10, Hoffman *et al.* ECCV'12, Csurka *et al.* Task-CV'14)
- ▶ Semi-supervised Transfer Component Analysis (Pan *et al.* TNN'11)

Structural Correspondence Learning⁹

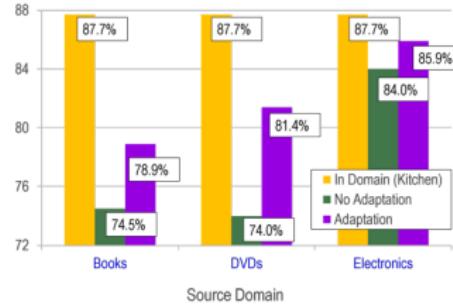
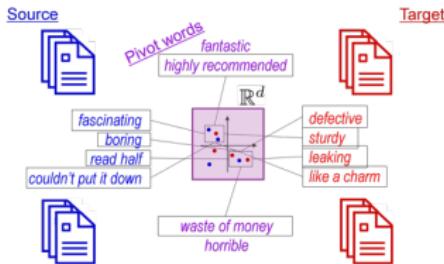


Image: Courtesy to Blitzer.

- ▶ Identify pivot features by mutual information between features and domains.
- ▶ Build P classifiers to predict the P pivot features from remaining features.
- ▶ Project to the shared subspace (using the top K eigenvectors).
- ▶ Concatenate with original features and train classifiers.

⁹

Blitzer *et al.*, Domain Adaptation with Structural Correspondence Learning, EMNLP'06

Spectral Feature Alignment¹⁰

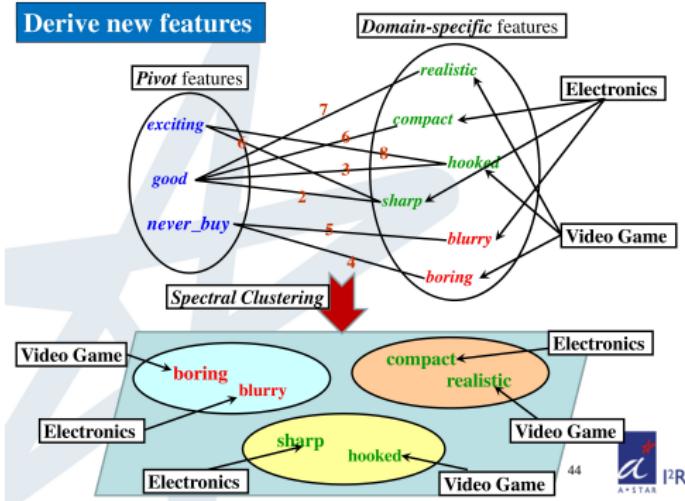
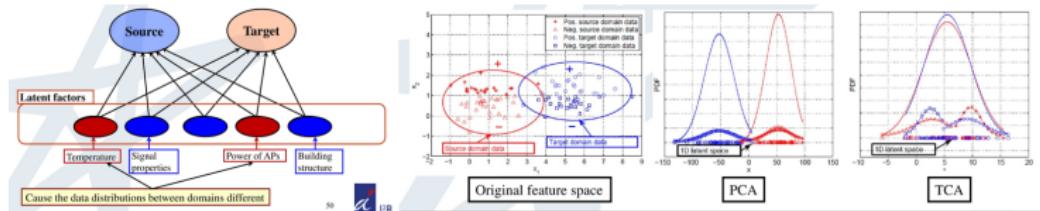


Image: Courtesy to Pan.

- ▶ Bipartite graph to model correlations between pivot features and the others.
- ▶ Discover new shared features by spectral clustering on the graph.

¹⁰ Pan et al., Cross-Domain Sentiment Classification via Spectral Feature Alignment, WWW'10

Transfer Component Analysis¹¹ (TCA)



To minimize the distance between domains

$$\min_W \text{tr}(W^T K L K W) + \lambda \text{tr}(W^T W)$$

s.t. $W^T K H K W = I$.

Regularization on W

To maximize the data variance

\downarrow

$W^* \Leftrightarrow m$ leading eigenvectors of $(K L K + \lambda I)^{-1} K H K$, where $m \leq n_S + n_T - 1$.

Image: Courtesy to Pan.

¹¹ Pan et al., Domain Adaptation via Transfer Component Analysis, IJCAI'09

Geodesic Flow Sampling¹² (GFS)

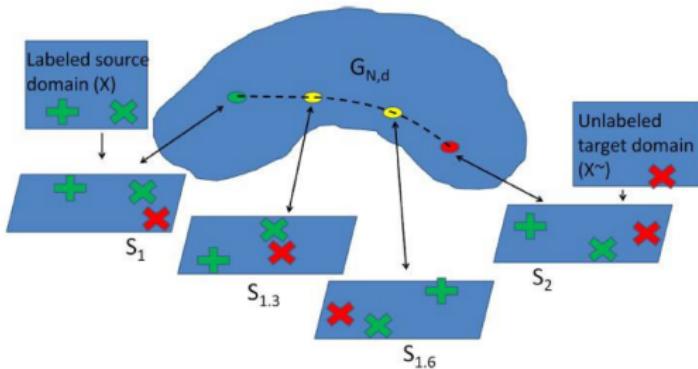


Image: Courtesy to Gopalan.

- ▶ Apply PCA on source data (\mathbf{S}_1 of rank d) and on the target (\mathbf{S}_2 of rank d).
- ▶ Geodesic path on the Grassman manifold $\mathbb{G}_{N,d}$ between \mathbf{S}_1 and \mathbf{S}_2 .
- ▶ Exponential flow $\psi(t') = \mathbf{Q}\exp(t'\mathbf{B})\mathbf{J}$ such that $\mathbf{Q}^\top \mathbf{S}_1 = \mathbf{J}$ and $\mathbf{J}^\top = [\mathbf{I}_d \mathbf{0}_{N-d,d}]$.
- ▶ Compute \mathbf{B} for intermediate subspaces varying $t \in [0, 1]$.

¹² Gopalan et al. Domain adaptation for object recognition: An unsupervised approach, ICCV'11.

Geodesic Flow Kernel¹³ (GFK)

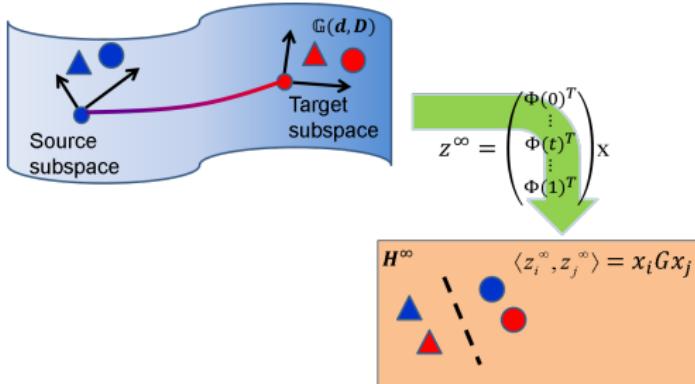


Image: Courtesy to Gong.

- Domain invariant features (infinite number of projections)

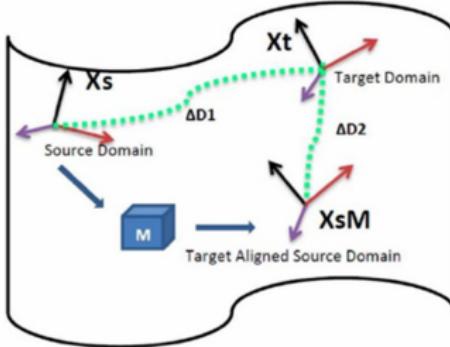
$$z^\infty = [\Phi(0)^\top \mathbf{x}, \dots, \Phi(t)^\top \mathbf{x}, \dots, \Phi(1)^\top \mathbf{x}]$$

- Use the kernel trick

$$\langle z_i^\infty, z^\infty \rangle = \int_0^1 (\Phi(t)^\top \mathbf{x})^\top (\Phi(t)^\top \mathbf{x}) dt = \mathbf{x}_i^\top \mathbf{G} \mathbf{x}_j$$

¹³ Gong et al., Geodesic flow kernel for unsupervised domain adaptation, CVPR'12.

Subspace Alignment¹⁴ (SA)



- $M^* = \mathbf{S}_1' \mathbf{S}_2$ corresponds to the “subspace alignment matrix”:
$$M^* = \operatorname{argmin}_M \| \mathbf{S}_1 M - \mathbf{S}_2 \|$$
- $X_a = \mathbf{S}_1 \mathbf{S}_1' \mathbf{S}_2 = \mathbf{S}_1 M^*$ projects the source data to the target subspace
- A natural similarity: $\text{Sim}(x_s, x_t) = x_s \mathbf{S}_1 M^* \mathbf{S}_1' x_t' = x_s \mathbf{A} x_t'$

Image: Courtesy to Fernando.

¹⁴ Fernando et al. Unsupervised Visual Domain Adaptation Using Subspace Alignment, ICCV'13.

Marginalized Denoising Autoencoders¹⁵ (MDA)

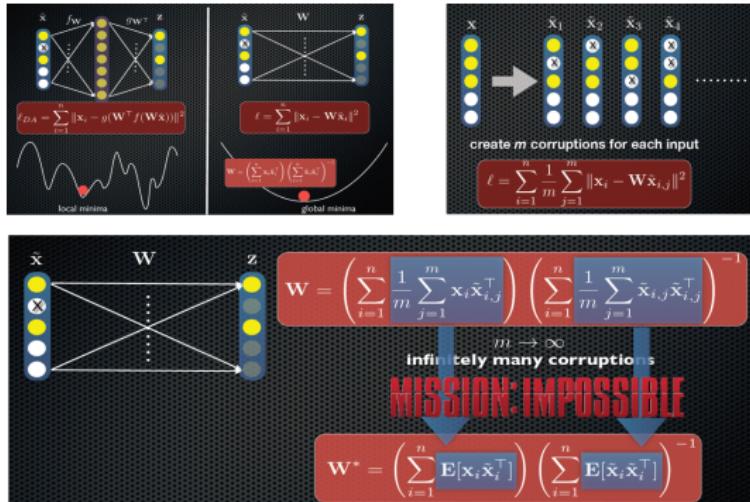


Image: Courtesy to Chen.

- ▶ Learns a direct mapping that allow closed form solution for a given corruption.
- ▶ Generates many (ideally infinity) corruptions for each input.

¹⁵ Chen et al., Marginalized Stacked Denoising Autoencoders for Domain Adaptation, ICML'12

- ▶ Marginalizes out the corruption (convergence to expected values), hence \mathbf{W} can be expressed in closed form as $W^* = \mathbb{E}[\mathbf{P}] \mathbb{E}[\mathbf{Q}]^{-1}$, where:

$$\mathbb{E}[\mathbf{P}]_{ij} = \mathbf{S}_{ij} q_j \quad \text{and} \quad \mathbb{E}[\mathbf{Q}]_{jj} = \begin{cases} \mathbf{S}_{ij} q_i q_j, & \text{if } i \neq j \\ \mathbf{S}_{ii} q_i, & \text{if } i = j \end{cases}$$

with:

- $q = [1 - p, \dots, 1 - p, 1] \in R^{n+1}$, p being the noise level and n the feature dimension
- $\mathbf{S} = \mathbf{X}\mathbf{X}^\top$ the covariance matrix of the uncorrupted data \mathbf{X}
- $\mathbf{X} = [\mathbf{x}_1, \dots, \mathbf{x}_m]$ where $\mathbf{x}_i = [\mathbf{x}_i, 1]$ for the inputs \mathbf{x}_i , where the constant is never corrupted

¹⁶Chen et al., Marginalized Stacked Denoising Autoencoders for Domain Adaptation, ICML'12

Stacked MDA¹⁷ (SMDA)

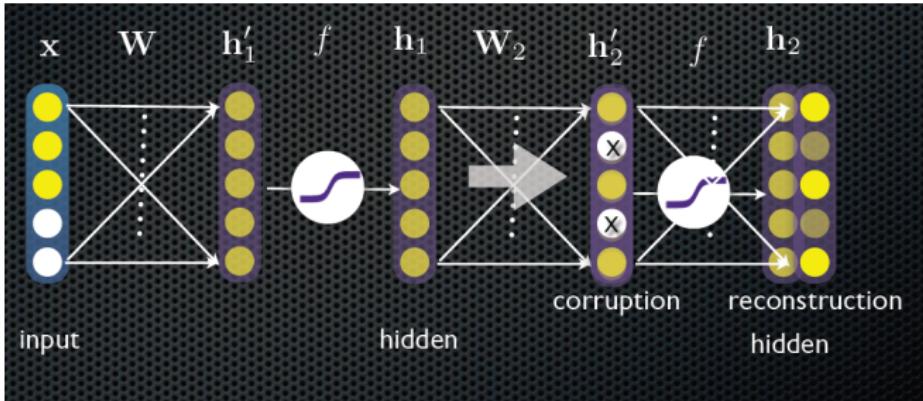


Image: Courtesy to M. Chen.

- ▶ Several MDA layers are stacked together
- ▶ Applying nonlinearities between layers helps
 - tangent-hyperbolic nonlinearities: $\mathbf{h}_t = \tanh(\mathbf{W}^t \mathbf{h}_{t-1})$

¹⁷ Chen et al., Marginalized Stacked Denoising Autoencoders for Domain Adaptation, ICML'12

Results on the OC10 (US sse) dataset



	C -> A	D -> A	W -> A	A -> C	D -> C	W -> C	A -> D	C -> D	W -> D	A -> W	C -> W	D -> W	Average
TCA	46.7	39.6	40.2	40	34	33.7	39.1	41.4	77.5	40.1	36.2	80.4	45.74
GFS	36.8	32	27.5	35.3	29.4	21.7	30.7	32.6	54.3	31	30.6	66	35.66
GFK (PCA)	36.9	32.6	31.3	35.6	29.8	27.3	35.2	35.2	70.6	34.4	33.7	74.9	39.79
GFK (PLS)	40.4	36.1	35.5	37.9	32.7	29.3	35.1	41.1	71.2	35.7	35.8	79.1	42.49
SA (SVM)	46.1	42	39.3	39.9	35	31.8	38.8	39.4	77.9	39.6	38.9	82.3	45.92
SMDA	49.85	37.05	37.26	41.99	36.65	33.93	37.17	45.59	73.31	37.28	43.7	80.3	46.17

- **TCA** - Transfer Component Analysis, Pan *et al.* IJCAI'09.
- **GFS** - Geodesic Flow Sampling, Gopalan *et al.* ICCV'11.
- **GFK** - Geodesic Flow Kernel, B. Gong *et al.* CVPR'12.
- **SA** - Subspace Alignment, Fernando *et al.* ICCV'13.
- **SMDA** - Stacked Marginalized Denoising Autoencoders, Chen *et al.* ICML'12.

Results on AMT

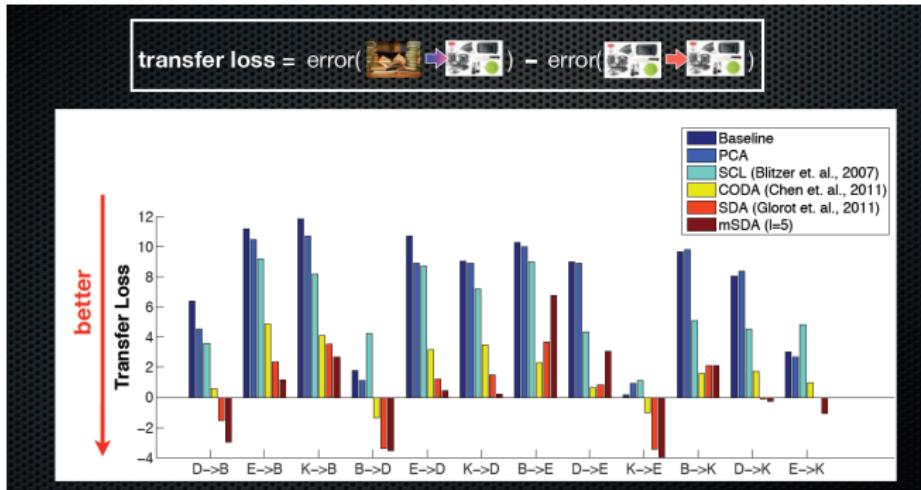
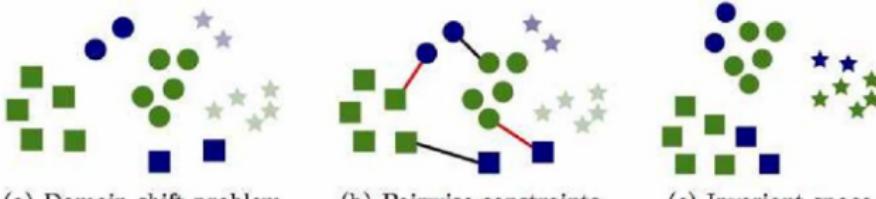


Image: Courtesy to M. Chen.

- **SCL** - Structural Correspondence Learning, Blitzer *et al.*, EMNLP'06.
- **SDA** - Deep learning approach - Glorot *et al.* ICML'11.
- **CODA** - Co-training for Domain Adaptation, Chen *et al.* NIPS'11.
- **mSDA** - Stacked Marginalized Denoising Autoencoders, Chen *et al.* ICML'12.

Information Theoretic Metric Learning¹⁸ (ITML)



(a) Domain shift problem

[Saenko et al.,ECCV'10]

(b) Pairwise constraints

(c) Invariant space

Formulation (based on ITML [Davis et al.,ICML'07])

$$\min_{\mathbf{W} \succeq 0} \quad Tr(\mathbf{W}) - \log \det \mathbf{W}$$

$$\text{s.t.} \quad d_{\mathbf{W}}^2(\mathbf{x}_i^s, \mathbf{x}_j^t) \leq u, \forall (\mathbf{x}_i^s, \mathbf{x}_j^t) \in \text{SimilarSet}$$

$$d_{\mathbf{W}}^2(\mathbf{x}_i^s, \mathbf{x}_j^t) \geq l, \forall (\mathbf{x}_i^s, \mathbf{x}_j^t) \in \text{DissimilarSet}$$

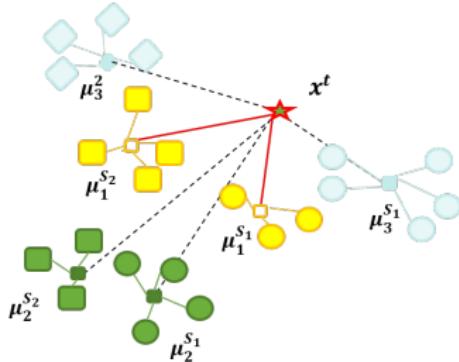
⇒ Can be kernelized

Image: Courtesy to Habrard.

¹⁸

Saenko et al., Adapting visual category models to new domains, ECCV 10

Domain Specific Class Means¹⁹ (DSCM)



The class label of a target is predicted based on

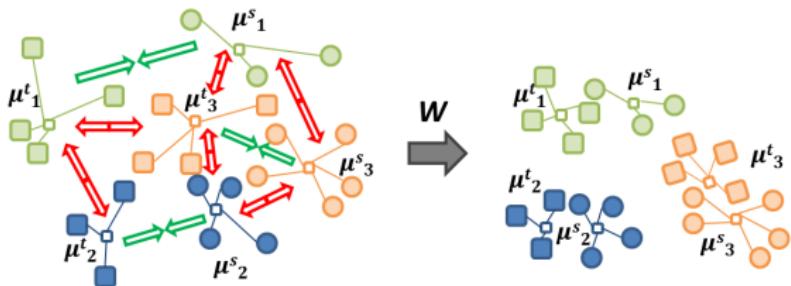
$$p(c|\mathbf{x}_i) = \frac{\sum_{d \in D} w_d e^{(-\frac{1}{2} \|\mathbf{x}_i - \boldsymbol{\mu}_d^c\|)}}{Z_i = \sum_{c'} \sum_d w_d e^{(-\frac{1}{2} \|\mathbf{x}_i - \boldsymbol{\mu}_d^{c'}\|)}}$$

where

- ▶ $\boldsymbol{\mu}_d^c$ is the mean of the class $c \in C$ in the domain $d \in D$
- ▶ w_d are domain specific weights (we used $w_{S_i} = 1$ and $w_t = 2$)

¹⁹ Csurka et al., Domain adaptation with a domain specific class means classifier. TASK-CV14

Metric Learning for DSCMs²⁰ (MLDSCM)



Mixture of GMM

$$p(c|\mathbf{x}_i) = \frac{\sum_d w_d \mathcal{N}(\mathbf{W}\mathbf{x}_i, \mathbf{W}\mu_d^c, \Sigma)}{\sum_{c'} \sum_d w_d \mathcal{N}(\mathbf{W}\mathbf{x}_i, \mathbf{W}\mu_d^{c'}, \Sigma)} = \frac{\sum_d w_d \exp\left(-\frac{1}{2}d_{\mathbf{W}}(\mathbf{x}_i, \mu_d^c)\right)}{\sum_{c'} \sum_d w_d \exp\left(-\frac{1}{2}d_{\mathbf{W}}(\mathbf{x}_i, \mu_d^{c'})\right)}$$

with

- ▶ domain-specific class means μ_d^c ,
- ▶ domain-specific weights w_d .

²⁰ G. Csurka *et al.* Domain Adaptation with a Domain Specific Class Means Classifier, Task-CV'14.

Semi-Supervised TCA²¹

The diagram shows the optimization function for Semi-Supervised TCA:

$$\min_W \text{tr}(W^\top K L K W) + \lambda_1 \text{tr}(W^\top W) + \frac{\lambda_2}{(n_S + n_T)^2} \text{tr}(W^\top K \mathcal{L} K W)$$

s.t. $W^\top K H K_{yy} H K W = I$

Annotations explain the components:

- To minimize the distance between domains
- To control the complexity of W
- Laplacian
- To maximize the data variance
- To preserve geometric locality
- To propagate label information
- To maximize the label dependence

Algorithm: generalized eigen decomposition

Image: Courtesy to Pan.

- \mathbf{K} is the (RBF) kernel matrix between the data points (both source and target)
- \mathcal{L} is the Laplacian of the affinity matrix $M_{i,j} = \exp(-d_{i,j}^2/2\sigma^2)$.
- \mathbf{K}_{yy} is a kernel matrix corresponding to source labels
- \mathbf{L} integrates the normalizations $1/N_S^2$, $1/N_T^2$ and $1/N_S N_T$ and \mathbf{H} is a centering matrix.

²¹ S.J. Pan *et al.*, Domain Adaptation via Transfer Component Analysis, TNN'11.

Results on the OC10 (SS sse) dataset



	C ->A	D ->A	W ->A	A ->C	D ->C	W ->C	A ->D	C ->D	W->D	A ->W	C ->W	D ->W	Average
ITML	33.7	30.3	32.3	27.3	22.5	21.7	33.7	35	51.3	36	34.7	55.6	34.51
MLDSCM	50.64	48.76	48.43	34.89	34.24	33.42	62.05	61.57	64.65	66.08	65.06	71.47	53.44
SSTCA	47.1	40.1	41.5	40.4	34.2	33.5	39	41.7	77.8	41.1	36.2	80.5	46.09

- **ITML** - Information Theoretic Metric Learning, Saenko *et al.*, ECCV'10
- **MLDSCM** - ML for Domain Specific Class Means, Csurka *et al.* Task-CV WS'14.
- **SSTCA** - Semi-Supervised TCA, Pan *et al.*, TNN'11.

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Methods combining several of the above ideas

- ▶ Joint feature and parameter adaptation
 - Max-Margin Domain Transforms (MMDT) of Hoffman *et al.* ICLR13
 - Naive Bayes NN based DA (NBNN-DA) of Tommasi and Caputo, ICCV13
 - Domain Invariant Projection (DIP-CC) of M. Baktashmotlagh *et al.* ICCV13
 - Joint Distribution Adaptation (JDA) of Long *et al.* ICCV 14
 - Transfer Joint Matching (TJM) of Long *et al.* ICCV 14
 - Optimal Transport for Domain Adaptation (OTDA) of Courty *et al.* PAMI 15
- ▶ Joint feature or instance selection and parameter adaptation
 - Feature selection and subspace learning (FSSL) of Gu *et al.* IJCAI 11
 - Landmark Selection (LM) of Gong *et al.* ICML13
 - Landmarks Selection-based SA (LSSA) of Aljundi CVPR15
- ▶ Joint instance selection, feature transform and parameter adaptation
 - Adaptive Transductive Transfer Machines (ATTM) of Farajidavar *et al.* BMVC 14
 - Statistically Invariant Embedding (SIE-CC) of M. Baktashmotlagh *et al.* CVPR 14

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Max-Margin Domain Transforms²² (MMDT)

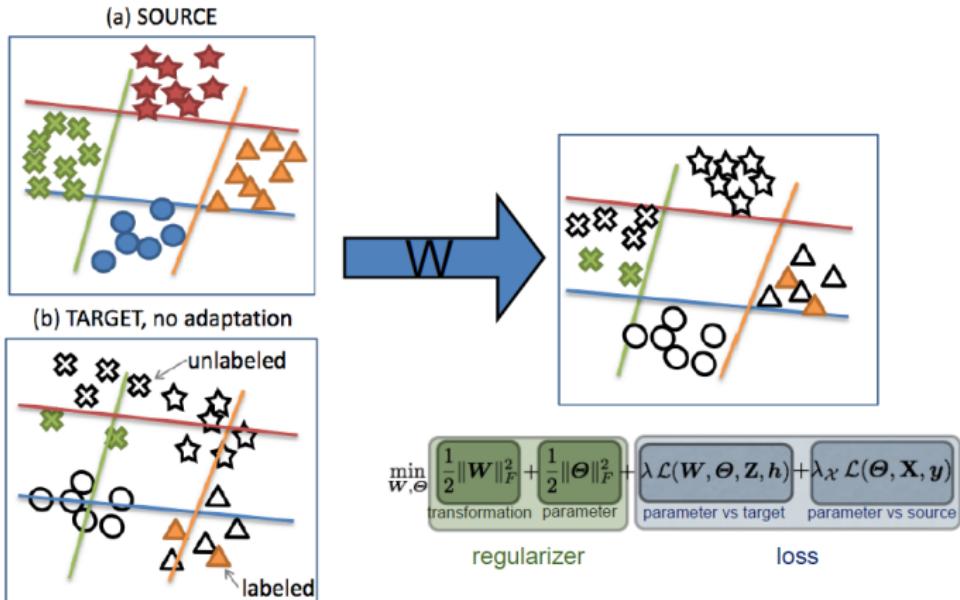


Image: Courtesy to Hoffman.

²²Hoffman et al., Max-margin transforms for visual domain adaptation, ICLR'13.

Naive Bayes NN based DA²³ (NBNN-DA)

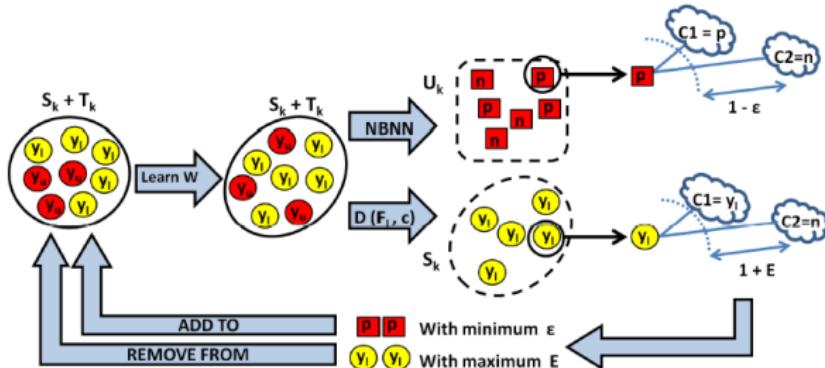


Image: Courtesy to Tommasi.

Iteratively combine metric learning and NBNN-based sample selection to:

- ▶ adjust the image-to-class distances by tuning the per class metrics
- ▶ iteratively making the metric progressively more suitable for the target

²³

Tommasi and Caputo, Frustratingly Easy NBNN Domain Adaptation, ICCV'13.

Transfer Joint Matching²⁴ (TJM)

Algorithm 1: TJM: Transfer Joint Matching

Input: Data \mathbf{X} ; #subspace bases k , regularization parameter λ .
Output: Adaptation matrix \mathbf{A} , embedding \mathbf{Z} , adaptive classifier f .

```
1 begin
2     Compute MMD matrix  $\mathbf{M}$  by Equation (5), and kernel matrix
3          $\mathbf{K}$  by  $K_{ij} \leftarrow K(\mathbf{x}_i, \mathbf{x}_j)$  where  $K(\cdot, \cdot)$  is a predefined kernel.
4     Set  $\mathbf{M} \leftarrow \mathbf{M}/\|\mathbf{M}\|_F$ ,  $\mathbf{G} \leftarrow \mathbf{I}$ .
5     repeat
6         Solve the generalized eigendecomposition problem in
7             Equation (9) and select the  $k$  smallest eigenvectors to
8                 construct the adaptation matrix  $\mathbf{A}$ , and  $\mathbf{Z} \leftarrow \mathbf{A}^T \mathbf{K}$ .
9         Update the sub-gradient matrix  $\mathbf{G}$  by Equation (10).
10    until Convergence
11    Return an adaptive classifier  $f$  trained on  $\{\mathbf{A}^T \mathbf{k}_i, y_i\}_{i=1}^{n_s}$ .
```

²⁴Long *et al.* Transfer Joint Matching for Unsupervised Domain Adaptation, CVPR'14.

Joint Distribution Adaptation²⁵ (JDA)

Algorithm 1: JDA: Joint Distribution Adaptation

Input: Data \mathbf{X} , \mathbf{y}_s ; #subspace bases k , regularization parameter λ .

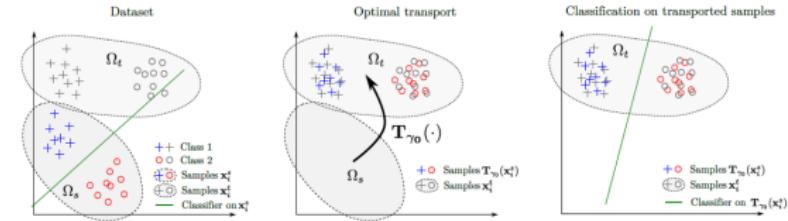
Output: Adaptation matrix \mathbf{A} , embedding \mathbf{Z} , adaptive classifier f .

```
1 begin
2   Construct MMD matrix  $\mathbf{M}_0$  by Eq. (4), set  $\{\mathbf{M}_c := \mathbf{0}\}_{c=1}^C$ .
3   repeat
4     Solve the generalized eigendecomposition problem in
      Equation (10) and select the  $k$  smallest eigenvectors to
      construct the adaptation matrix  $\mathbf{A}$ , and  $\mathbf{Z} := \mathbf{A}^T \mathbf{X}$ .
5     Train a standard classifier  $f$  on  $\{(\mathbf{A}^T \mathbf{x}_i, y_i)\}_{i=1}^{n_s}$  to
      update pseudo target labels  $\{\hat{y}_j := f(\mathbf{A}^T \mathbf{x}_j)\}_{j=n_s+1}^{n_s+n_t}$ .
6     Construct MMD matrices  $\{\mathbf{M}_c\}_{c=1}^C$  by Equation (6).
7   until Convergence
8   Return an adaptive classifier  $f$  trained on  $\{\mathbf{A} \mathbf{x}_i, y_i\}_{i=1}^{n_s}$ .
```

²⁵

M. Long *et al.* Transfer Feature Learning with Joint Distribution Adaptation, ICCV'14

Optimal Transport for Domain Adaptation²⁶ (OTDA)



Algorithm 1 Conditional gradient splitting (CCS)

```
1: Initialize  $k = 0$  and  $\gamma^0 \in \mathcal{P}$ 
2: repeat
3:   With  $\mathbf{G} \in \nabla f(\gamma^k)$ , solve

$$\gamma^* = \operatorname{argmin}_{\gamma \in \mathcal{B}} \langle \gamma, \mathbf{G} \rangle_F + g(\gamma)$$

4:   Find the optimal step with  $\Delta\gamma = \gamma^* - \gamma^k$ 

$$\alpha^k = \operatorname{argmin}_{0 \leq \alpha \leq 1} f(\gamma^k + \alpha\Delta\gamma) + g(\gamma^k + \alpha\Delta\gamma)$$

5:    $\gamma^{k+1} \leftarrow \gamma^k + \alpha^k\Delta\gamma$ , set  $k \leftarrow k + 1$ 
6: until Convergence
```

Image: Courtesy to Courty.

²⁶

N. Courty *et al.*, Optimal Transport for Domain Adaptation, CoRR'15.

Domain Invariant Projection²⁷ (DIP-CC)

- ▶ Optimizing the MMD on the Grassman manifold $\mathcal{G}(d, D)$

$$D_{\mathcal{H}}(\mathbf{W}^\top \mathbf{X}_S, \mathbf{W}^\top \mathbf{X}_T) = \left\| \frac{1}{N_s} \sum_{i=1}^{N_s} \phi(\mathbf{W}^\top \mathbf{x}_i^s) - \frac{1}{N_t} \sum_{j=1}^{N_t} \phi(\mathbf{W}^\top \mathbf{x}_j^t) \right\|_{\mathcal{H}}$$

where \mathbf{W} is a point on \mathcal{G} with the constraint $\mathbf{W}^\top \mathbf{W} = \mathbf{I}$.

- ▶ Adding term to encourage Class Clustering (CC) :

$$\sum_{c=1}^C \sum_{i=1}^{n_c} \|\mathbf{W}^\top (\mathbf{x}_{i,c}^s - \mu_c)\|^2$$

- ▶ The whole yielding to the optimization problem:

$$\boxed{\begin{aligned} \mathbf{W}^* &= \underset{\mathbf{W}}{\operatorname{argmin}} \quad Tr(K_W L) + \lambda \sum_{c=1}^C \sum_{i=1}^{n_c} \left\| \mathbf{W}^\top (\mathbf{x}_{i,c}^s - \mu_c) \right\|^2 \\ \text{s.t. } & \mathbf{W}^\top \mathbf{W} = \mathbf{I}, \end{aligned}} \quad \boxed{\begin{aligned} K_W &= \begin{bmatrix} K_{s,s} & K_{s,t} \\ K_{t,s} & K_{t,t} \end{bmatrix} \in \mathbb{R}^{(n+m) \times (n+m)} \\ L_{ij} &= \begin{cases} 1/n^2 & i, j \in \mathcal{S} \\ 1/m^2 & i, j \in \mathcal{T} \\ -1/(nm) & \text{otherwise} \end{cases}, \end{aligned}}$$

²⁷ M. Baktashmotlagh *et al.*, Unsupervised Domain Adaptation by Domain Invariant Projection, ICCV'13.

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Feature selection and subspace learning²⁸ (FSSL)



(d) Selected
features

file attachments

Algorithm 2 Joint Feature Selection and Subspace Learning (Situation 2)

Initialize: $G_0 = I$, $t = 0$ and μ ;
Compute Y based on $WY = \Lambda D Y$;
repeat
 Compute $A_{t+1} = G_t^{-1} X (X^T G_t^{-1} X + \frac{1}{2\mu} I)^{-1} Y$;
 Compute G_{t+1} based on A_{t+1} ;
 $t = t + 1$;
until convergence

Image: Courtesy to Gu.

²⁸

Gu, et al. Joint feature selection and subspace learning, IJCAI'11.

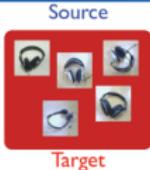
Landmark Selection²⁹

Landmarks are labeled **source** instances distributed similarly to the **target** domain.

Identifying landmarks:

$$P_{\mathcal{L}}(\text{landmarks}) \approx P_{\mathcal{T}}(\text{target})$$
$$\min_{\text{landmarks}} d(P_{\mathcal{L}}, P_{\mathcal{T}})$$

[Gong et al., ICML'13]



Convex relaxation

$$\min_{\{\alpha_m\}} \left\| \frac{1}{\sum_i \alpha_i} \sum_{m=1}^M \alpha_m \phi(x_m) - \frac{1}{N} \sum_{n=1}^N \phi(x_n) \right\|_{\mathcal{H}}^2$$

$$\beta_m = \frac{\alpha_m}{\sum_i \alpha_i}$$

$$\min_{\beta} \beta^T K^s \beta - \frac{2}{N} \beta^T K^{st} \mathbf{1}$$

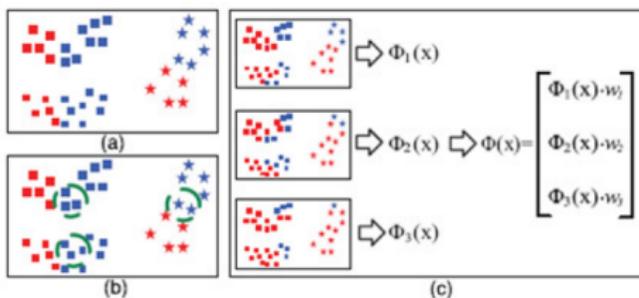


Image: Courtesy to Gong.

²⁹ Gong et al., Connecting the dots with landmarks: Discriminatively learning domain invariant features for unsupervised domain adaptation, ICML'13.

Landmarks Selection-based SA³⁰ (LSSA)

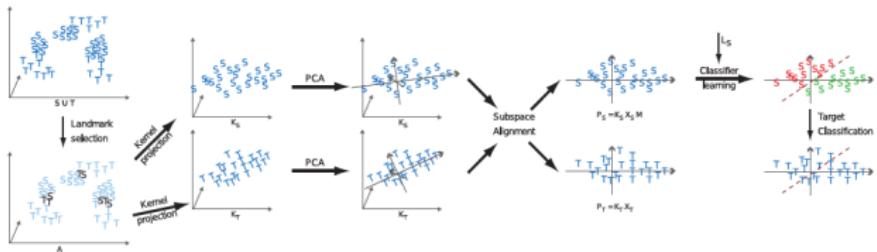


Image: Courtesy to Aljundi.

- ▶ Landmark selection using a Gaussian Kernels and overlap between the probability densities:

$$\text{overlap}(\mu_S, \sigma_S; \mu_T, \sigma_T) = \frac{\mathcal{N}(\mu_S - \mu_T | 0, (\sigma_S + \sigma_T)^2)}{\mathcal{N}(0 | 0, (\sigma_S + \sigma_T))}$$

- ▶ Subspace Alignment using the selected landmarks and linear SVM classifiers.

³⁰ Aljundi et al., Landmarks-based Kernelized Subspace Alignment for Unsupervised Domain Adaptation, CVPR'15.

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Transductive Transfer Machines³¹ (ATTM)

TTM Diagram



ATTM Algorithm

Input: $\mathbf{X}^{src}, \mathbf{Y}^{src}, \mathbf{X}^{trg}$

Output: \mathbf{Y}^{trg}

1. Search for the shared subspace between the two domains
2. Adjust the marginal distribution mismatch between the two domains
3. Select the appropriate classifier, if it is kernel-based, tune σ using
while $T < 10$ and $|D_{global}(G^t(\mathbf{X}^{src}), \mathbf{X}^{trg})| > threshold$ **do**
 4. Find the feature-wise TST transformation
 5. Transform the source domain clusters
 6. Retrain the classifier using the transformed source**end while**

Image: Courtesy to deCampos.

³¹

Farajidavar *et al.*, Adaptive Transductive Transfer Machines, BMVC'14.

Statistically Invariant Embedding³² (SIE-CC)



Image: Courtesy to Baktashmotagh.

► Statistically Invariant Sample Selection

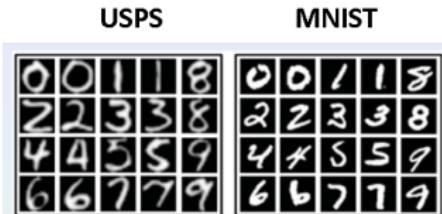
$$\begin{aligned} \min_{\beta} \sum_{i=1}^{n_s} \beta_i & \left(\sqrt{T(x_i^s)} - \sqrt{1 - T(x_i^s)} \right)^2 + \frac{1}{n_t} \sum_{i=1}^{n_t} \left(\sqrt{T(x_i^t)} - \sqrt{1 - T(x_i^t)} \right)^2 \\ \text{s.t. } \beta_i & \in [0, 1]; \quad \sum_{i=1}^{n_s} \beta_i = 1; \quad \sum_{i=1}^{n_s} \beta_i y_{i,c} = \frac{1}{n_s} \sum_{i=1}^{n_s} y_{i,c} \quad \forall c \end{aligned}$$

► Statistically Invariant Embedding

$$\begin{aligned} \min_{\mathbf{W}} D_{\mathcal{H}}(\mathbf{W}^\top \mathbf{X}_S, \mathbf{W}^\top \mathbf{X}_T) + \lambda \sum_{c=1}^C \sum_{i=1}^{n_c} & \|\mathbf{W}^\top (\mathbf{x}_{i,c}^s - \mu_c)\|^2 \\ \text{s.t. } \mathbf{W}^\top \mathbf{W} & = \mathbf{I} \end{aligned}$$

³² Baktashmotagh *et al.*, Domain Adaptation on the Statistical Manifold, CVPR'14.

Digit recognition results



	GFK	TCA	FSSL	TJM	JDA	OTDA	ATTM
U -> M	46.45	51.05	51.45	52.25	59.65	58.3	61.15
M -> U	67.22	56.28	57.44	63.28	67.28	69.39	77.9

- **GFK** - Geodesic Flow Kernel, B. Gong *et al.* CVPR'12.
- **TCA** - Transfer Component Analysis, Pan *et al.* IJCAI'09.
- **FFSL** - Feature selection and subspace learning, Gu *et al.* IJCAI'11.
- **TJM** - Transfer Joint Matching, Long *et al.* CVPR'14.
- **JDA** - Joint Distribution Adaptation, Long *et al.* ICCV'14.
- **OTDA** - Optimal Transport for Domain Adaptation, Courty *et al.* CoRR'15.
- **ATTM** - Adaptive Transductive Transfer Machines, Farajidavar *et al.*, BMVC'14.

Object recognition (OC10 US base)



	C->A	W->A	A->C	W->C	A->D	C->D	W->D	A->W	C->W	avg
SMDA	52.8	35.3	41.9	32.3	37.8	47.2	77.9	37	49.8	45.79
SA	52.7	39.4	41.6	34.7	46.4	49	78.9	40.7	42.7	47.34
LSSA	58.4	39.4	44.8	34.7	42.4	54.1	87.2	42.4	48.1	50.17
LS	56.7	40.2	45.5	35.4	47.1	57.3	75.2	46.1	49.5	50.3
TJM	58.6	40.8	45.7	34.8	42	49	83.4	42	48.8	49.45
JDA	44.8	32.8	39.4	31.2	39.5	45.2	89.2	38	41.7	44.62
OTDA	48	40	38.6	37.2	45	45.2	93	41.4	44.7	48.08
ATTM	60.8	39.7	42.9	34	31.8	50.3	89.2	50.5	38	48.59
DIP-CC	58.7	40.9	47.2	37.2	49	61.2	91.7	47.8	58	54.63
SIE-CC	57.6	42.4	47.6	36.2	49	61.2	93	47.8	57.3	54.68

- **SMDA** - Stacked Marginalized Denoising Autoencoders, Chen *et al.* ICML'12.
- **SA** - Subspace Alignment, Fernando *et al.* ICCV'13.
- **LSSA** - Landmarks Selection-based SA, Aljundi *et al.* CVPR'15.
- **LS** - Landmark Selection, Gong *et al.* ICML'13.
- **TJM** - Transfer Joint Matching, Long *et al.* CVPR'14.
- **JDA** - Joint Distribution Adaptation, long *et al.* ICCV'14.
- **OTDA** - Optimal Transport for Domain Adaptation, Courty *et al.* CoRR'15.
- **ATTM** - Adaptive Transductive Transfer Machines, Farajidavar *et al.*, BMVC'14.
- **DIP-CC** Domain Invariant Projection, Baktashmotlagh *et al.* ICCV'13.
- **SIE-CC** - Statistically Invariant Embedding, Baktashmotlagh *et al.* CVPR'14.

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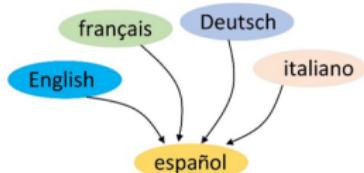
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Example: cross-lingual text categorization

- Experiments on the Reuters multilingual dataset



● Dataset				
	Domain	# dim. after PCA	# total docs	# training docs per class
Source	English	1,131	18,758	100
	French	1,230	26,648	100
	German	1,417	29,953	100
	Italian	1,041	24,039	100
Target	Spanish	807	11,547	5/7/10/15/20

● Means and standard deviations of classification accuracies (%) of all methods on the Reuters multilingual dataset by using 10 labeled training samples per class from the target domain Spanish. Results in boldface are significantly better than the others, judged by the t-test with a significance level at 0.05.

Source Domain	SVM-T	KCCA	HeMap	DAMA	ARC-t	HFA
English		71.4 ± 3.2	65.7 ± 3.1	72.4 ± 2.4	72.9 ± 2.0	75.3 ± 1.7
French		72.8 ± 2.8	64.2 ± 4.2	72.8 ± 2.0	73.5 ± 1.8	75.7 ± 1.6
German	72.6 ± 2.3	73.8 ± 2.2	64.6 ± 3.6	72.9 ± 2.3	74.7 ± 1.6	76.1 ± 1.5
Italian		73.8 ± 2.1	65.8 ± 2.3	73.3 ± 2.1	74.0 ± 2.0	75.8 ± 1.8

Image: Courtesy to Dong Xu.

Heterogeneous Feature Augmentation³³ (HFA)

- Objective

- The dual form is similar to SVM with a different kernel.

$$\begin{aligned} \min_{\mathbf{P}, \mathbf{Q}} \max_{\boldsymbol{\alpha}} \quad & \mathbf{1}'_{n_s+n_t} \boldsymbol{\alpha} - \frac{1}{2} (\boldsymbol{\alpha} \circ \mathbf{y}) \boxed{\mathbf{K}_{\mathbf{P}, \mathbf{Q}}} (\boldsymbol{\alpha} \circ \mathbf{y}) \\ \text{s.t. } & \mathbf{y}' \boldsymbol{\alpha} = 0, \quad \mathbf{0}_{n_s+n_t} \leq \boldsymbol{\alpha} \leq C \mathbf{1}_{n_s+n_t}, \\ & \|\mathbf{P}\|_F^2 \leq \lambda_p, \quad \|\mathbf{Q}\|_F^2 \leq \lambda_q. \end{aligned}$$

- Global optimum can be solved using the method similarly as in MKL (see our T-PAMI 2014 work for more details)

$\mathbf{X}_s'(\mathbf{I}_{n_s} + \mathbf{P}'\mathbf{P})\mathbf{X}_s$	$\mathbf{X}_s'\mathbf{P}'\mathbf{Q}\mathbf{X}_t$
$\mathbf{X}_t'\mathbf{Q}'\mathbf{P}\mathbf{X}_s$	$\mathbf{X}_t'(\mathbf{I}_{n_t} + \mathbf{Q}'\mathbf{Q})\mathbf{X}_t$

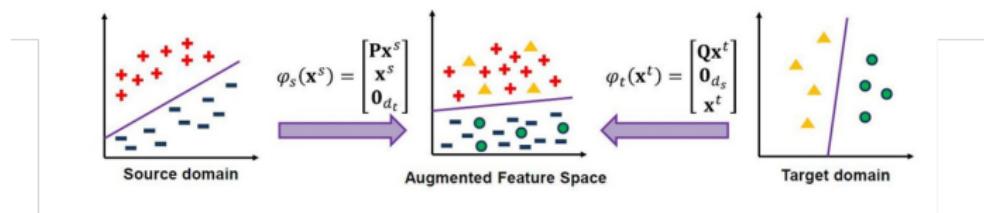


Image: Courtesy to Dong Xu.

- Generalizes the feature replication method of Daume III, ACL 07.

³³Duan et al. Learning with Augmented Features for Heterogeneous Domain Adaptation, CVPR12.

Dictionary-based Approaches

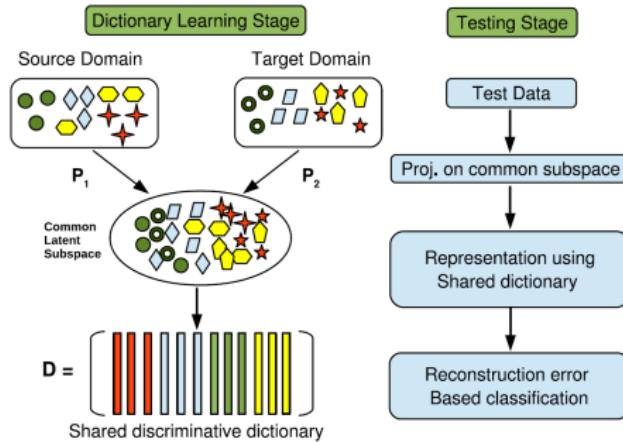


Image: Courtesy to S. Shekhar.

- ▶ Each domain has its own projection matrix.
- ▶ Can be used when features in source and target are different.
- ▶ Generalizes well to multiple sources.

Shared Domain-adapted Dictionary Learning³⁴ (SDDL)

- Main idea:

$$\{\mathbf{D}^*, \tilde{\mathbf{W}}^*, \tilde{\mathbf{X}}^*\} = \underset{\mathbf{D}, \tilde{\mathbf{W}}, \tilde{\mathbf{X}}}{\operatorname{argmin}} \mathcal{C}_1(\mathbf{D}, \tilde{\mathbf{W}}, \tilde{\mathbf{X}}) + \lambda \mathcal{C}_2(\tilde{\mathbf{W}})$$

s.t. $\mathbf{W}_i \mathbf{W}_i^T = \mathbf{I}$, $i = 1, 2$ and $\|\tilde{\mathbf{x}}_j\|_0 \leq T_0, \forall j$

$$\tilde{\mathbf{W}} = [\mathbf{W}_1 \ \mathbf{W}_2], \quad \tilde{\mathbf{Y}} = \begin{pmatrix} \mathbf{S} & \mathbf{0} \\ \mathbf{0} & \mathbf{T}_l \end{pmatrix}, \text{ and } \tilde{\mathbf{X}} = [\mathbf{X}_1 \ \mathbf{X}_2].$$

$$\mathcal{C}_1(\mathbf{D}, \tilde{\mathbf{W}}, \tilde{\mathbf{X}}) = \|\tilde{\mathbf{W}} \tilde{\mathbf{Y}} - \mathbf{D} \tilde{\mathbf{X}}\|_F^2,$$

$$\mathcal{C}_2(\tilde{\mathbf{W}}) = -\text{trace}((\tilde{\mathbf{W}} \tilde{\mathbf{Y}})(\tilde{\mathbf{W}} \tilde{\mathbf{Y}})^T)$$

- Its kernelized extension

$$\begin{aligned} \mathcal{C}_1(\tilde{\mathbf{A}}, \tilde{\mathbf{B}}, \tilde{\mathbf{X}}) &= \|\tilde{\mathbf{A}}^T \mathcal{K} (\mathbf{I} - \tilde{\mathbf{B}} \tilde{\mathbf{X}})\|_F^2 + \\ &\mu \|\tilde{\mathbf{A}}^T \mathcal{K} (\mathbf{I} - \tilde{\mathbf{B}} \tilde{\mathbf{X}}_{in})\|_F^2 + \nu \|\tilde{\mathbf{A}}^T \mathcal{K} \tilde{\mathbf{B}} \tilde{\mathbf{X}}_{out}\|_F^2, \\ \mathcal{C}_2(\tilde{\mathbf{A}}) &= -\text{trace}((\tilde{\mathbf{A}}^T \mathcal{K})(\tilde{\mathbf{A}}^T \mathcal{K})^T) \end{aligned}$$

³⁴ Shekhar et al., Generalized Domain-Adaptive Dictionaries, CVPR 13.

Results on the OC10 (SS sse)



	C ->A	D ->A	W ->A	A ->C	W ->C	C ->D	A ->W	D ->W	Average
FDDL	39.3	36.7	41.1	24.3	22.9	55	50.4	65.9	38.5
SDDL	49.5	48.9	49.4	27.4	29.7	76.7	72	72.6	53.3
MLDSCM	50.64	48.76	48.43	34.89	33.42	61.57	66.08	71.47	51.9
DIP-CC	61.8	56.9	53.4	47.8	43.6	65.8	72.5	89.1	61.36

- **FDDL** Fisher Discrimination Dictionary Learning, Yang *et al.* ICCV'11.
- **SDDL** Shared Domain-adapted Dictionary Learning, Shekhar *et al.* CVPR 13.
- **MLDSCM** - ML for Domain Specific Class Means, Csurka *et al.* Task-CV WS'14.
- **DIP-CC** Domain Invariant Projection, Baktashmotagh *et al.* ICCV'13.

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Joint instance selection, feature and parameter adaptation

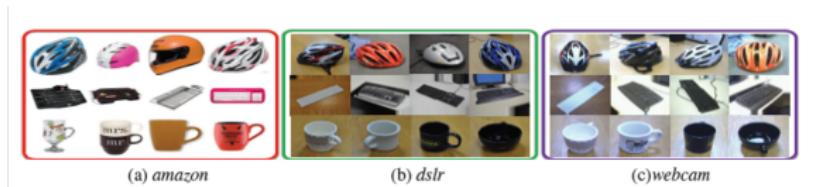
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Multi-sources results on the OFF31 (SS sse)



(SS)				(US)					
	A ,D->W	A,W ->D	D,W->A	Avg		A ,D->W	A,W ->D	D,W->A	Avg
DSCM	58.21	57.65	21.67	45.84	DSCM	45.04	35.51	12.12	30.89
SDDL	57.8	56.7	24.1	46.2	GFS	37.5	33.9	31.5	34.3
BGFS	64.5	51.3	38.4	51.4	SSF	47.8	49.6	40.2	45.87
HL2L	66.1	67.9	25.8	53.27					

- **DSCM** - Domain Specific Class Means, Csurka *et al.* Task-CV'14.
- **SDDL** Shared Domain-adapted Dictionary Learning, Shekhar *et al.* CVPR 13.
- **GFS** - Geodesic Flow Sampling, Gopalan *et al.* ICCV'11.
- **BGFS** - Boosted Geodesic Flow Sampling, Gopalan *et al.* CoRR'15.
- **HL2L** - High-level Learning to Learn, Patricia and Caputo, CVPR'14.
- **SSF** - Spline Flow Sampling, Caseiro *et al.* CVPR'15.

Boosted Geodesic Flow Sampling³⁵ (BGFS)

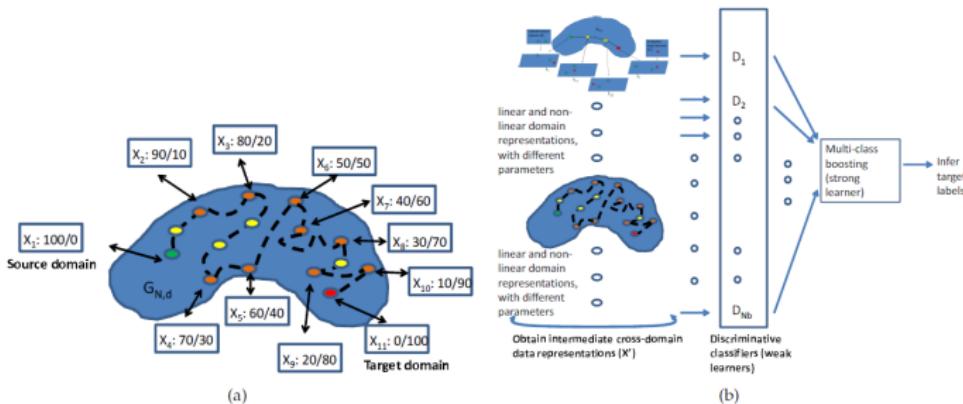


Image: Courtesy to Gopalan.

- ▶ Intermediate "domains" between source and target on the Grassman Manifold
- ▶ Multi-domain adaptation using Karcher mean of domains
- ▶ Jointly learn domain shift features and classifiers with AdaBoost

³⁵ Gopalan et al. Unsupervised Adaptation Across Domain Shifts By Generating Intermediate Data Representations, CoRR'15.

Spline Flow Sampling³⁶ (SSF)

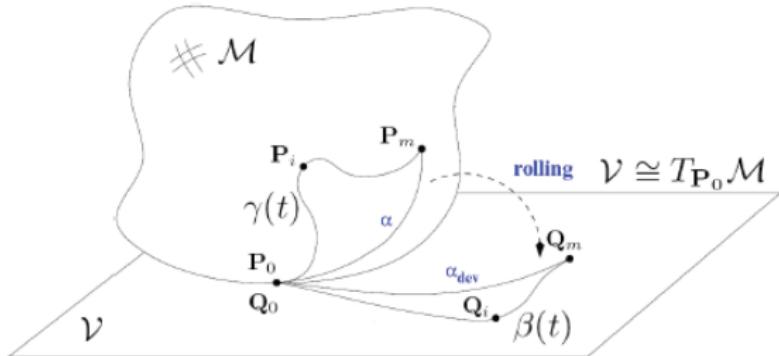


Image: Courtesy to Caseiro.

- ▶ $\alpha(t) : [0, T] \mapsto \mathcal{M}$ the rolling geodesic curve on the manifold \mathcal{M}
- ▶ $\beta(t) : [0, T] \mapsto \mathcal{V}$ the spline curve on the tangent space \mathcal{V}
- ▶ $\gamma(t) : [0, T] \mapsto \mathcal{M}$ the spline curve on the manifold \mathcal{M}

³⁶ Caseiro et al. Beyond the shortest path : Unsupervised Domain Adaptation by Sampling Subspaces along the Spline Flow, CVPR 15.

High-level Learning to Learn³⁷ (H-L2L)

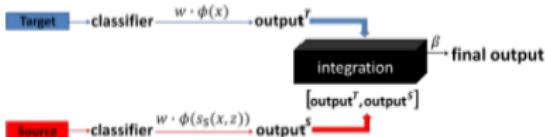


Image: Courtesy to Patricia.

Boosting approach to learn β_y^c where the weak learners are:

$$s(\mathbf{x}, y) = \beta^0 \mathbf{w}_0 \phi^0(\mathbf{x}, y) + \sum_{c=1}^{N_C} \beta_y^c \mathbf{w}_y^c \phi_y^c(s_S(\mathbf{x}, c), y)$$

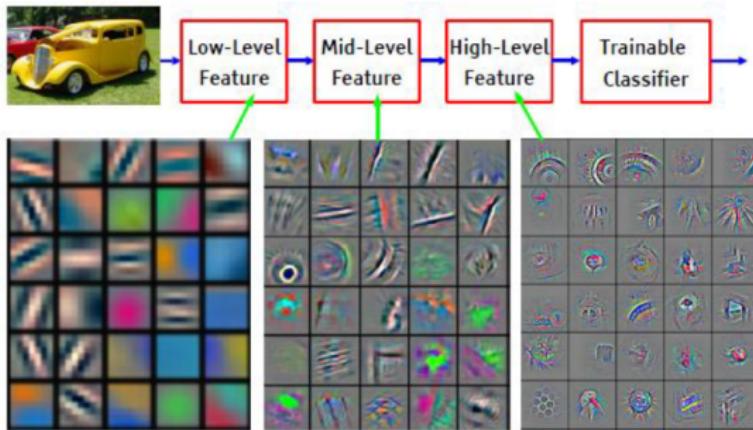
- ▶ $s_S(\mathbf{x}, c)$ the score of \mathbf{x} with the source classifier c
- ▶ $\phi_y^c \mapsto Y \times Y$ is the y^{th} score mapping corresponding to the c^{th} source model
- ▶ \mathbf{w}_y^c the $y - th$ source model in predicting that \mathbf{x} belongs to class c
- ▶ $\phi^0(\mathbf{x}, y)$ is the feature mapping for the original input features

³⁷ Patricia and Caputo, Learning to Learn, from Transfer Learning to Domain Adaptation: A Unifying Perspective, CVPR 14.

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What about deep features?



Deep Learning:
More than one
stage of non-
linear feature
transformation

Image: Courtesy to Y LeCun H.

- ▶ High-non linearity makes these features more invariant across domains!

Deep convolutional activation features³⁸ (DeCAF)

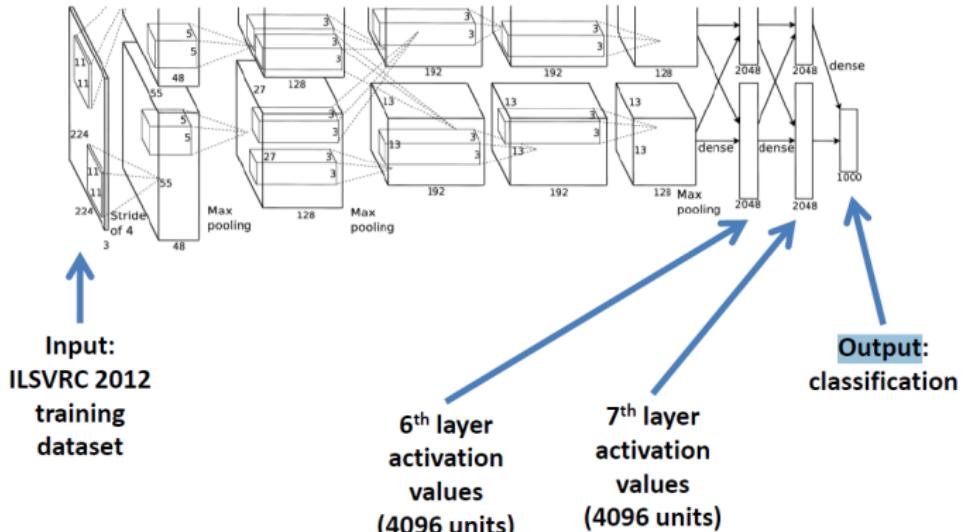
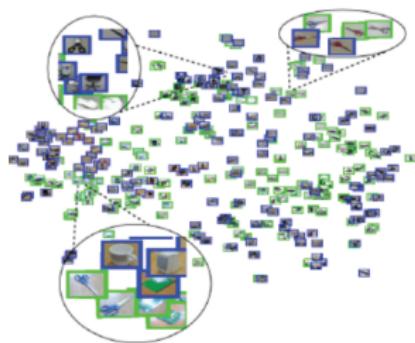


Image: Courtesy to A. Krizhevsky.

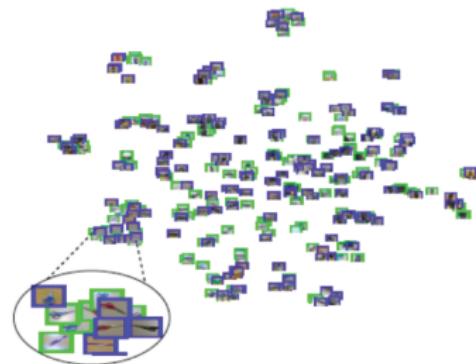
- ▶ CNN model pre-trained on big data (ImageNet)
- ▶ use convolutional activation layers as features.

³⁸Donuahe *et al.* DeCAF: A deep convolutional activation feature for generic visual recognition, ICML 14

Compared to bag of visual-words³⁹ (BOV)



(a) SURF features



(b) DeCAF₆

Image: Courtesy to Donuahe.

- ▶ DeCAF provides better category level clustering than SURF BOV

³⁹

G. Csurka *et al.* Visual categorization with bags of keypoints, SLCV 2004.

Results on OFF31 (US sse)

		bike	desk chair				
(D)	dslr						
(A)	amazon						
(W)	webcam						

	A ->W	D ->W	W->D	Avg
NN	42.8	86.4	88.6	72.6
SVM	63.05	95.04	96.74	84.94
NCM	64.76	92.17	94.37	83.77
SMDA	68.56	92.92	95.01	85.5
GFK	46.8	87.2	88.1	74.03
TCA	44.6	89	87.9	73.83
SA	47.2	91.8	92.4	77.13

- **NN** - Nearest Neighbor classifier (no adaptation).
- **SVM** - Linear SVM classifier (no adaptation).
- **NCM** - Nearest Class Means classifier (DSCM with single domain, no adaptation).
- **SMDA** - Stacked Marginalized Denoising Autoencoders, Chen *et al.* ICML'12.
- **GFK** - Geodesic Flow Kernel, B. Gong *et al.* CVPR'12.
- **TCA** - Transfer Component Analysis, Pan *et al.* IJCAI'09.
- **SA** - Subspace Alignment, Fernando *et al.* ICCV'13.

Results on OC10 (US sse)



	C ->A	C ->W	C ->D	A ->C	A ->W	A ->D	W->C	W->A	W->D	D ->C	D ->A	D ->W	Avg
NN	85.7	66.1	74.52	70.35	64.97	57.29	60.37	62.53	98.73	52.09	62.73	89.15	70.33
SVM	94.61	85.28	87.4	88.47	86.79	88.98	86	87.28	100	84.81	87.28	98.4	89.61
NCM	94.07	87.55	87.4	88.2	87.17	85.04	87.01	90.3	99.21	85.82	90.52	98.49	90.6
SMDA	93.86	90.19	88.98	89.48	87.92	88.98	89.48	93.64	99.21	89.02	93.32	99.25	91.94
JDA	89.77	83.73	86.62	82.28	78.64	80.25	83.53	90.19	100	85.13	91.44	98.98	87.55
ATTM	92.17	90.84	92.99	86.55	89.15	90.45	83.44	92.27	100	82.28	91.65	98.98	90.9

- **NN** - Nearest Neighbor classifier (no adaptation).
- **SVM** - Linear SVM classifier (no adaptation).
- **NCM** - Nearest Class Means classifier (DSCM with single domain, no adaptation).
- **SMDA** - Stacked Marginalized Denoising Autoencoders, Chen *et al.* ICML'12.
- **JDA** - Joint Distribution Adaptation, long *et al.* ICCV'14.
- **ATTM** - Adaptive Transductive Transfer Machines, Farajidavar *et al.*, BMVC'14.

Interpolating between Domains⁴⁰ (DLID)

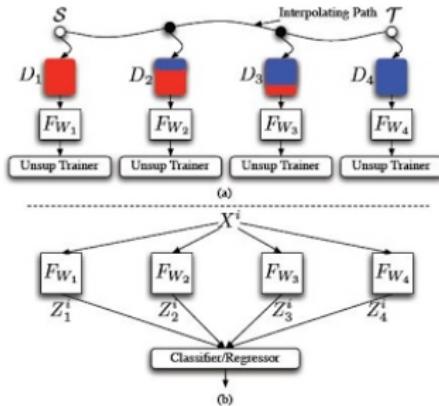


Image: Courtesy to S. Chopra

- ▶ generate intermediate datasets D_p by mixing target and source
- ▶ unsupervised deep nonlinear extractor $\mathbf{F}_{\mathbf{W}_p}$ learned on
- ▶ train classifiers on the concatenated features $\mathbf{Z}_p^i = \mathbf{F}_{\mathbf{W}_i}(\mathbf{X}^i)$.

⁴⁰ S. Chopra et al. Deep Learning for domain adaptation by Interpolating between Domains, RL-WS ICML13.

Deep Domain Confusion⁴¹ (DDC)

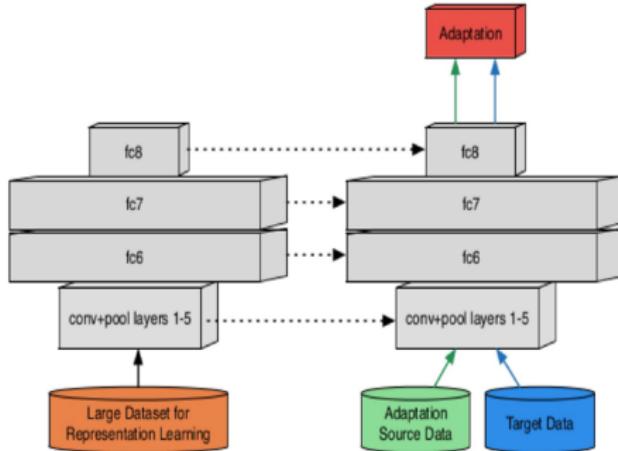


Image: Courtesy to E. Tzeng

- ▶ Minimizing the loss

$$\mathcal{L} = \mathcal{L}_C(X_L, y) + \lambda \text{MMD}^2(X_S, X_T)$$

⁴¹

E. Tzeng et al., Deep Domain Confusion: Maximizing for Domain Invariance, CoRR 14.

Deep Adaptation Networks⁴² (DAN)

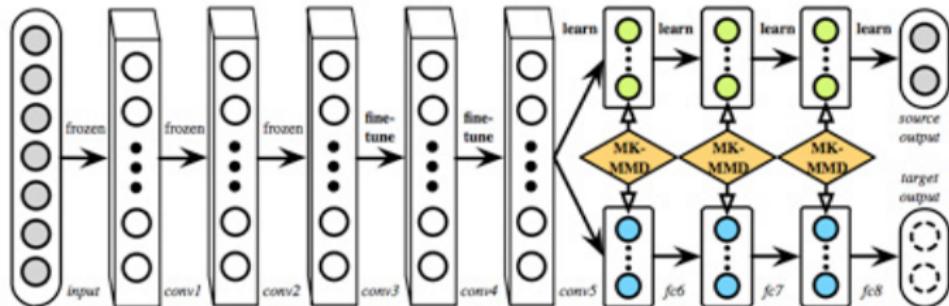


Image: Courtesy to M. Long

- ▶ first 3 convolutional layers are kept frozen
- ▶ next 2 convolutional layers refined with the current dataset
- ▶ deeply adapt fc6-fc8 using Multiple Kernel MMD

⁴²

M. Long et al., Learning Transferable Features with Deep Adaptation Networks, CoRR'15.

Domain Adaptation by Backpropagation⁴³ (DAB)

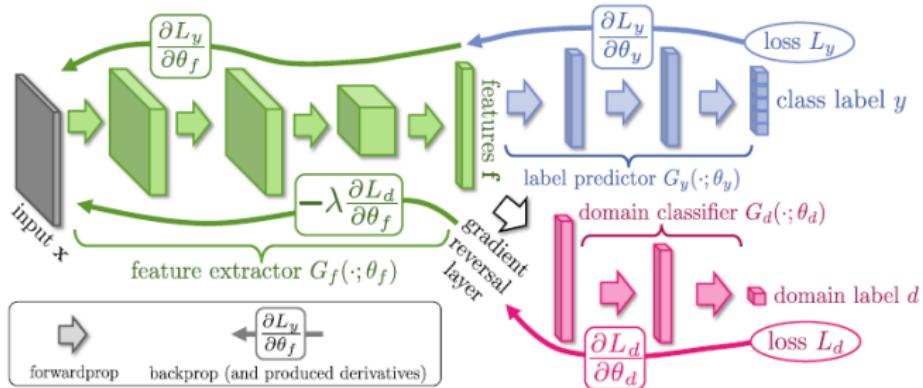


Image: Courtesy to Y. Ganin.

- ▶ L_y is the loss for label prediction (e.g. multinomial),
- ▶ L_d is the loss for the domain classification (e.g. logistic),

⁴³ Y. Ganin and V. Lempitsky, Unsupervised Domain Adaptation by Backpropagation, ICML 15.

Results on OFF31 (US sse)

	bike	desk chair		A ->W	D ->W	W->D	Avg	
dslr				SMDA	69.8	94.44	97.28	87.17
amazon				DLID	51.9	78.2	89.9	73.33
webcam				DDC	60.5	94.8	98.5	84.6
				DAN	64.5	95.2	98.6	86.1
				DAB	73	96.4	99.2	89.53

- **SMDA** - Stacked Marginalized Denoising Autoencoders, Chen *et al.* ICML'12.
- **DLID** - Interpolating between Domains Chopra *et al.* RL-WS ICML13.
- **DDC** - Deep Domain Confusion, Tzeng *et al.* CoRR'14.
- **DAN** - Deep Adaptation Networks, Long *et al.*, CoRR'15.
- **DAB** - Domain Adaptation by Backpropagation, Ganin and Lempitsky, ICML'15.

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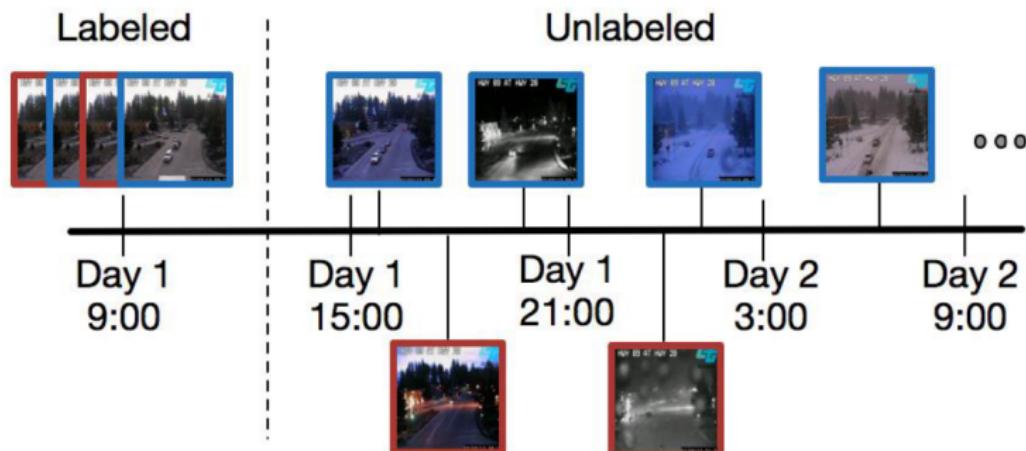
Conclusion

- ▶ Many method exploits the Maximum Mean Discrepancy (MMD)
- ▶ Most popular methods are based on feature transform
 - Manifold based methods (GFS, GFK, BGFK)
 - Unsupervised subspace alignment (SA, LSSA)
 - Stacked marginalized denoising autoencoders (SMDA)
- ▶ Best performing methods exploit jointly instance selection, feature transform and parameter adaptation
 - Adaptive Transductive Transfer Machines (ATTM)
 - Statistically Invariant Embedding (SIE-CC)
- ▶ DeCAF features yield to significantly better results
 - Adding adaptation methods can further improve the results.
 - Using Deep Learning to perform adaptation performs the best.

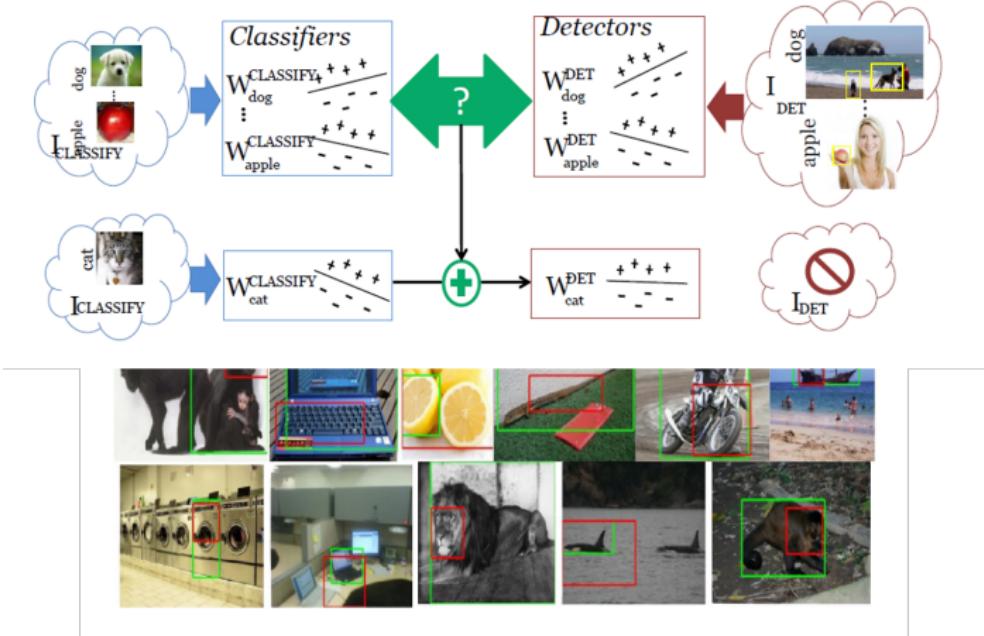
More challenging transfer problems



Continuous adaptation



Adapting object detection⁴⁴



⁴⁴

Hoffman et al. LSDA: Large Scale Detection Through Adaptation, NIPS'14.

Adapting video action recognition⁴⁵



- ▶ adapting between single and double, between tennis and badminton

⁴⁵ N. Farajidavar *et al.*, Domain Adaptation in the Context of Sport Video Action Recognition, NIPSW DA , 2011.
<http://cvssp.org/acasva/Downloads.html>



Thank you !